

Quiz #1

1. Determine the derivatives of each of the following functions.

a. $f(x) = 5x^3 - x$

b. $g(x) = \sqrt[3]{x}$

2. Let $f(x) = 5x^2 - 3x + 18$. **Use the limit definition of the derivative** to show that $f'(x) = 10x - 3$. (Note: You are being graded on notation, so write out each step clearly).

3. The following is partial table of values for a function $P(t)$.

x	0	1	2	3	4	5
$g(x)$	11	10	7	2	-5	-14

a. Use the central difference quotient to estimate $g'(2)$.

b. Use the central difference quotient to estimate $g'(1.5)$.

4. Determine the equation of the line tangent to the graph of $f(x) = \frac{4}{x^2}$ at the point $x = 2$.

5. The temperature in degrees Fahrenheit of a cup of coffee is given by $f(t)$ where t is the minutes since the coffee was poured into the cup. Give the meaning of the following statements in plain English (including all appropriate units).

a. $f(5) = 90$

b. $f'(5) = -3$

c. $f'(5) < 0$ and $f''(5) > 0$

6. Sketch a possible graph of $f(x)$

$f(x)$ is continuous and differentiable $(-\infty, \infty)$

$$f'(x) > 0 \quad -4 < x < 6$$

$$f'(x) < 0 \quad x < -4 \text{ or } x > 6$$

$$f''(x) > 0 \quad x < 1$$

$$f''(x) < 0 \quad x > 1$$

